



Key Figures 2010

PSI funds (global budget)	249	MCHF
External funding	~ 60	MCHF
Staff	~ 1400	PJ
Of which externally financed	~ 370	PJ
Doctoral students	~ 300	
Apprentices	80	
External users	~ 2000	
Number of scientific publications	~ 900	
PSI-employees with teaching duties at ETH and universities	~ 80	

Precise Beam Dynamics Simulations: from High Power Cyclotron to (X)FEL Modeling

A. Adelman (PSI-AMAS)

Acknowledgments: Y. Ineichen Ch. Kraus (PSI)

Y. Bi, J. Yang, Ch. Wang (CIAE) &
S. Russel (LANL)

SwissFEL Folks: B. Beutner, A. Falone, G L Orlandi and T. Schietinger

LBL - Wednesday, March 9 2011

Outline

- 1 Motivation & Problem Setup
- 2 The Models upon OPAL is based
- 3 OPAL and its Flavours
- 4 Simulation Results
 - Precise Simulations of the PSI Ring Cyclotron
 - Particle Matter Interaction
 - Multipacting & Dark Current Modeling
- 5 The SwissFEL & the 250 MeV Accelerator Test Facility

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Why Precise Beam Dynamics Simulations?

- consider a n MW (Cyclotron) proton driver - understanding halo
- H_2^+ versus a scheme with p (DAE δ ALUS)
- compact XFEL
 - providing 6D phase space at the undulator
 - bunch compression is a 3D process
 - transverse deflecting cavities
 - dark current & non uniform emission
 - many challenges of Bruce

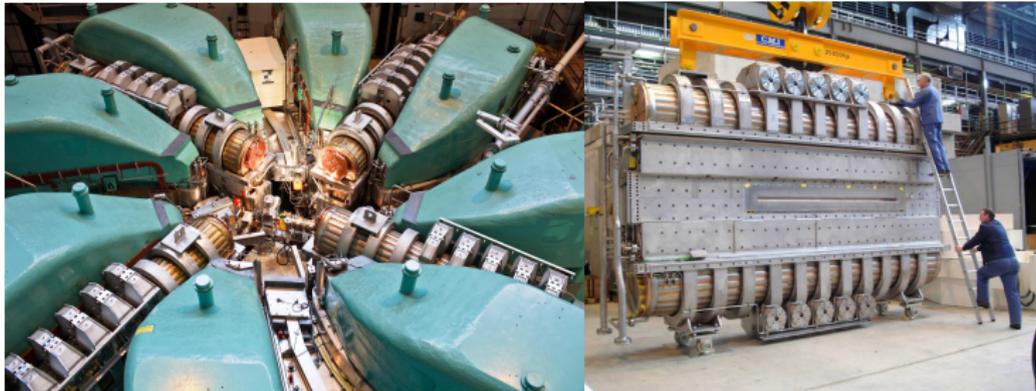
Dark Current Simulations

(Dark Current)

The High Intensity Challenge

Consider a 0.59 GeV, 2.3 mA (CW) Proton Cyclotron facility.

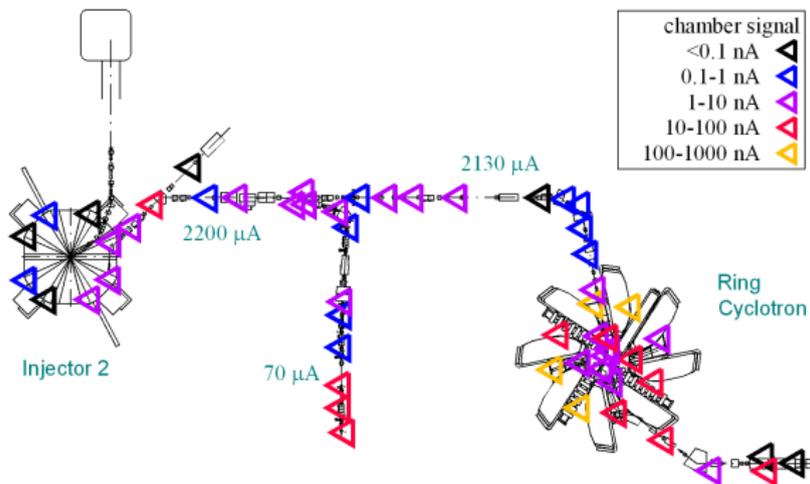
- uncontrolled & controlled beam loss $\mathcal{O}(2\mu\text{A} = \text{const})$ in large and complex structures
- PSI Ring: 99.98% transmission $\rightarrow \mathcal{O}(10^{-4}) \rightarrow 4\sigma$
- small changes at injection affects extraction



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Consequences for a Beam Dynamics Model

- Multiscale / Multiresolution
 - Maxwell's equations or **reduced set** combined with particles
 - N-body problem $n \sim 10^9$ per bunch in case of PSI
 - Spatial scales: $10^{-4} \dots 10^4$ (m) $\rightarrow \mathcal{O}(1e5)$ integration steps
 - $v \ll c \dots v \sim c$
 - Large (complicated structures)
 - Neighboring bunches
- Multiphysics
 - Particle matter interaction: monte carlo
 - Secondary particles i.e. multi specis

Given an appropriate **physics model** it is necessary to combining state of the art **numerical methods** together with a **massively parallel implementation**.

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Collision-less (non relativistic) Vlasov-Maxwell equation

$f_s \subset (\mathbb{R}^3 \times \mathbb{R}^3), \mathbb{R}^3 \rightarrow \mathbb{R}^3$ and s are the species.

$$\frac{\partial f_s}{\partial t} + \mathbf{v} \cdot \nabla_x f_s + \frac{q_s}{m_s} (\mathbf{E} + \mathbf{v} \times \mathbf{B}) \cdot \nabla_v f_s = 0,$$

$$\left. \begin{aligned} \frac{\partial \mathbf{E}}{\partial t} - c^2 \mathbf{curl} \mathbf{B} &= \frac{\mathbf{J}}{\epsilon_0}, & \operatorname{div} \mathbf{E} &= \frac{\rho}{\epsilon_0}, \\ \frac{\partial \mathbf{B}}{\partial t} + \mathbf{curl} \mathbf{E} &= 0, & \operatorname{div} \mathbf{B} &= 0, \end{aligned} \right\} \text{Maxwell's equations}$$

where the source terms are computed by

$$\rho = \sum_s q_s \int f_s d\mathbf{v}, \quad \mathbf{J} = \sum_s q_s \int f_s \mathbf{v} d\mathbf{v}.$$

The electric and magnetic fields \mathbf{E} and \mathbf{B} are superpositions of external fields and self-fields (space charge),

$$\mathbf{E} = \mathbf{E}_{\text{ext}} + \mathbf{E}_{\text{sc}}, \quad \mathbf{B} = \mathbf{B}_{\text{ext}} + \mathbf{B}_{\text{sc}}.$$

If \mathbf{E} and \mathbf{B} are known, then each particle can be propagated according to the equation of motion for charged particles in an electromagnetic field,

$$\frac{d\mathbf{x}(t)}{dt} = \mathbf{v}, \quad \frac{d\mathbf{v}(t)}{dt} = \frac{q}{m_0} (\mathbf{E} + \mathbf{v} \times \mathbf{B}).$$

Maxwell's Equation in the Electrostatic approximation

Field Maps &
Analytic Models

Electro
Magneto
Optics

$$\mathbf{H} = \mathbf{H}_{\text{ext}} + \mathbf{H}_{\text{sc}}$$

$$\begin{aligned} \operatorname{div} \mathbf{E}_{\text{sc}} &= \rho / \epsilon_0 = \operatorname{div} \nabla \phi_{\text{sc}} \\ \Delta \phi_{\text{sc}} &= -\frac{\rho}{\epsilon_0} \\ &\text{\& BC's} \end{aligned}$$

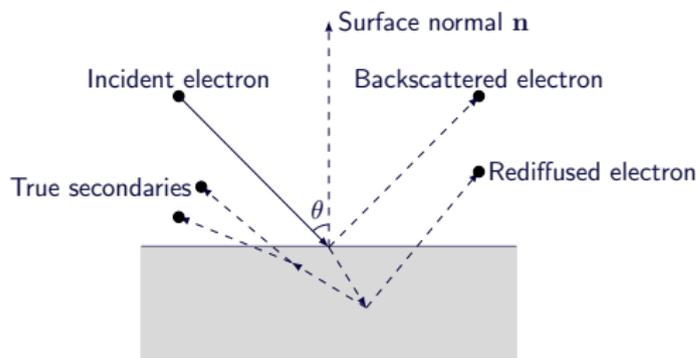
N-Body
Dynamics

With G the 3D open space Green's function $G(\mathbf{x}, \mathbf{x}') = \frac{1}{\sqrt{(\mathbf{x}-\mathbf{x}')^2}}$ the solution of the Poisson equation at point \mathbf{x} can be expressed by

$$\phi_{\text{sc}}(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \int G(\mathbf{x}, \mathbf{x}') \rho(\mathbf{x}, \mathbf{x}') d\mathbf{x}'.$$

Particle Matter Interaction & Space Charge

- Energy loss $-dE/dx$ (Bethe-Bloch)
- Coulomb scattering is treated as two independent events:
 - multiple Coulomb scattering
 - large angle Rutherford scattering
- Field Emission Model (Fowler-Nordheim)
- Secondary Emission Model ([Furman & Pivi] & [Vaughan])



- Phenomenological- don't involve secondary physics but fit the data.
- Model 1 developed by M. Furmann and M. Pivi
- Model 2 (Vaughan) is easier to adapt to SEY curves

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OPAL in a Nutshell

OPAL is a tool for charged-particle optics in large accelerator structures and beam lines including 3D space charge and particle matter interaction

- OPAL is built from the ground up as a parallel application exemplifying the fact that HPC (High Performance Computing) is the third leg of science, complementing theory and the experiment
- OPAL runs on your laptop as well as on the largest HPC clusters
- OPAL uses the MAD language with extensions
- OPAL (and all other used frameworks) are written in C++ using OO-techniques, hence OPAL is very easy to extend.
- Documentation is taken very seriously at both levels: source code and user manual (<http://amas.web.psi.ch/docs/index.html>)
- Regression tests running every day on the head of the repository

www.amas.psi.ch

OPAL and its Flavours

4 OPAL flavours exist:

- OPAL-T
 - OPAL-T tracks particles which 3D space charge uses time as the independent variable, and can be used to model beamlines, guns, injectors and complete FEL's but without the undulator.
 - Field emission (dark current studies)
 - many more linac features ...
- OPAL-ENVELOPE
 - OPAL-ENVELOPE is based on the 3D-envelope equation (à la HOMDYN) and can be used to design FEL's.
 - OPAL-ENVELOPE could also be used for an on-line model (incl. space charge)
 - same lattice than OPAL-T
- OPAL-MAP (not yet released)
 - OPAL-MAP tracks particles with 3D space charge using split operator techniques.
 - $\mathcal{M}(s) = \mathcal{M}_{\text{ext}}(s/2) \otimes \mathcal{M}_{\text{sc}}(s) \otimes \mathcal{M}_{\text{ext}}(s/2) + \mathcal{O}(s^3)$

OPAL and its Flavours cont.

- OPAL-CYCL
 - 3D space charge
 - neighboring turns
 - time is the independent variable.
 - from p to Uranium (q/m is a parameter)
 - Solve Poisson equation with spectral methods
 - Use 4th-order RK and Leap Frog
 - Single particle tracking mode & tune calculation
 - Particle Matter Interaction
 - Multipacting capabilities

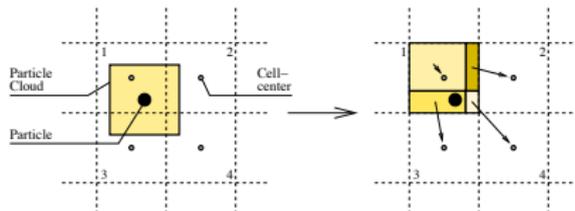
OPAL is developed by an international collaboration including Los Alamos (LANL), China Institute of Atomic Energy (CIAE) and Tsinghua University, Beijing.

Parallel I/O (H5hut) PSI-LBL collaboration.

A fast Direct FFT-Based Poisson Solver

Solving for ϕ using $\phi(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \int G(\mathbf{x}, \mathbf{x}')\rho(\mathbf{x}, \mathbf{x}')d\mathbf{x}'$ is expensive $\mathcal{O}(N^2)$ with N number of particles.

- 1 Discretize $\rho \rightarrow \rho_h$ and $G \rightarrow G_h$ on a regular grid (PIC).



- 2 Go to Fourier space $\rho_h \rightarrow \hat{\rho}_h$, $G_h \rightarrow \hat{G}_h$ and convert the convolution into a multiplication $\mathcal{O}(\log N)$.
- 3 Use a parallel FFT, particle and field load balancing.

Iterative Poisson Solver SAAMG-PCG

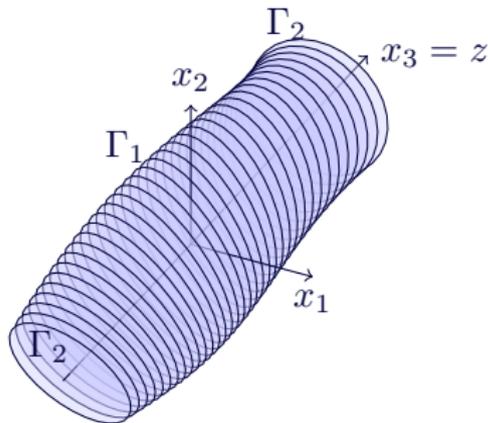
Boundary Problem

$$\Delta\phi = -\frac{\rho}{\varepsilon_0}, \text{ in } \Omega \subset \mathbb{R}^3,$$

$$\phi = 0, \text{ on } \Gamma_1$$

$$\frac{\partial\phi}{\partial\mathbf{n}} + \frac{1}{d}\phi = 0, \text{ on } \Gamma_2$$

- $\Omega \subset \mathbb{R}^3$: simply connected computational domain
- ε_0 : the dielectric constant
- $\Gamma = \Gamma_1 \cup \Gamma_2$: boundary of Ω
- d : distance of bunch centroid to the boundary



Γ_1 is the surface of an

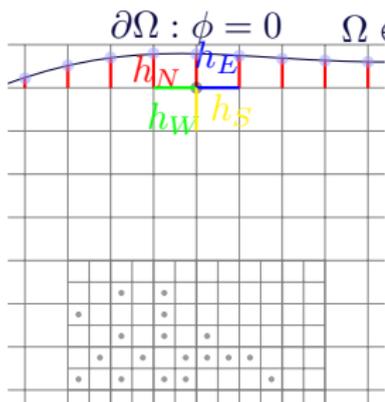
- 1 elliptic beam-pipe
- 2 arbitrary beam-pipe element

Iterative Poisson Solver SAAMG-PCG cont.

We apply a second order finite difference scheme which leads to a set of linear equations

$$\mathbf{Ax} = \mathbf{b},$$

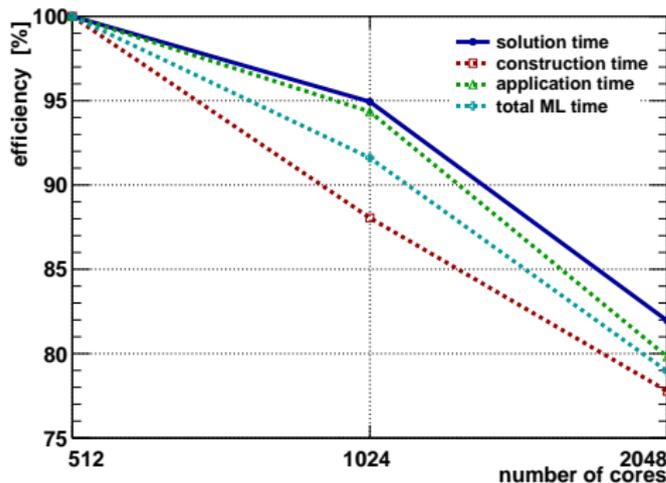
where \mathbf{b} denotes the charge densities on the mesh.



- solve anisotropic electrostatic Poisson PDE with an iterative solver
- reuse information available from previous time steps
- achieving good parallel efficiency
- irregular domain with “exact” boundary conditions
- easy to specify boundary surface

[A. Adelman, P. Arbenz and Y. Ineichen]

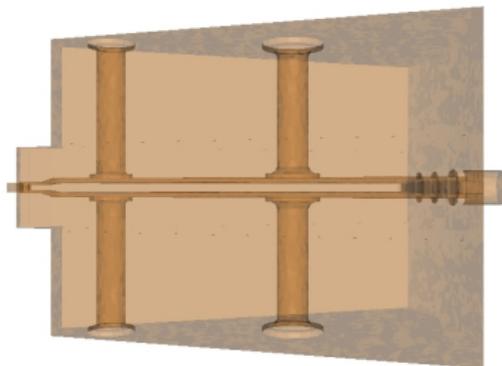
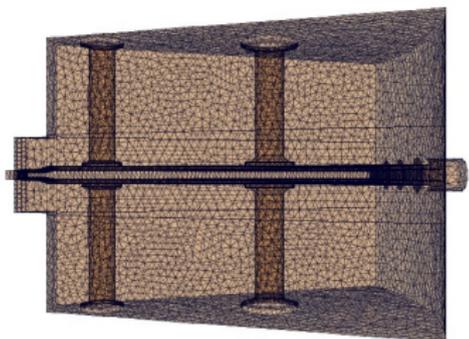
SAAMG-PCG Parallel Efficiency



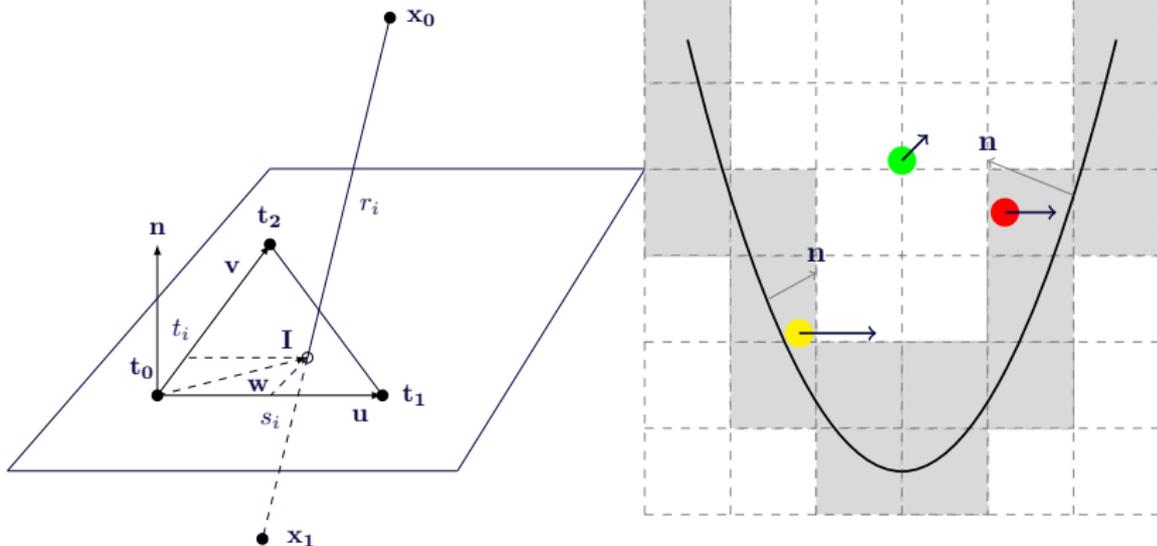
- obtained for a tube embedded in a $1024 \times 1024 \times 1024$ grid
- construction phase is performing the worst with an efficiency of 73%
- influence of problem size on the low performance of the aggregation in ML

3D Geometry Handling Capability of OPAL

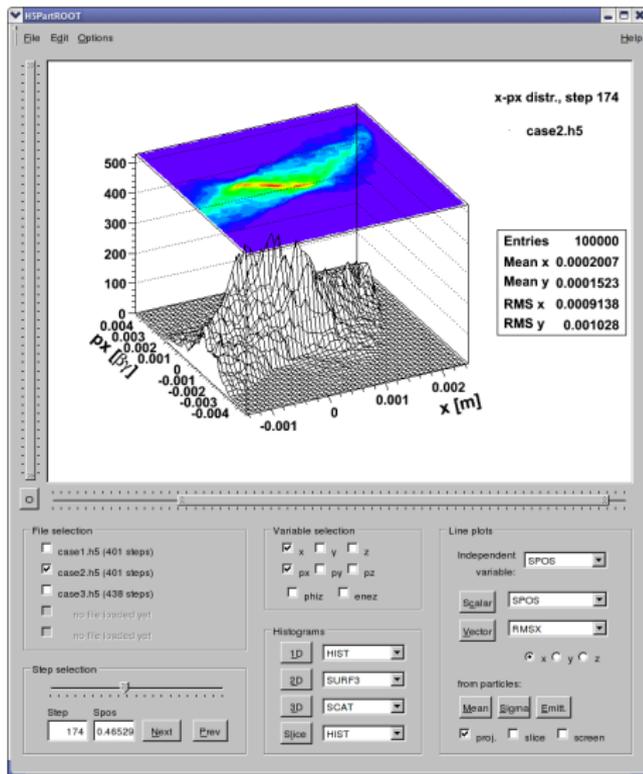
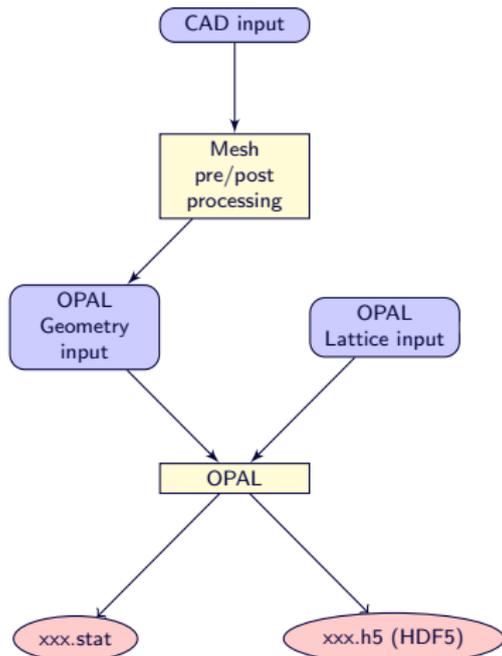
- Read in surface mesh generated by Heronion or GMSH
- Triangulated surface representation of geometry



- Triangle-line segment intersection
- Boundary bounding box to speedup the collision tests
- We can handle arbitrary structure as long as it is closed



Parallel I/O (H5hut) & Postprocessing (H5Root)



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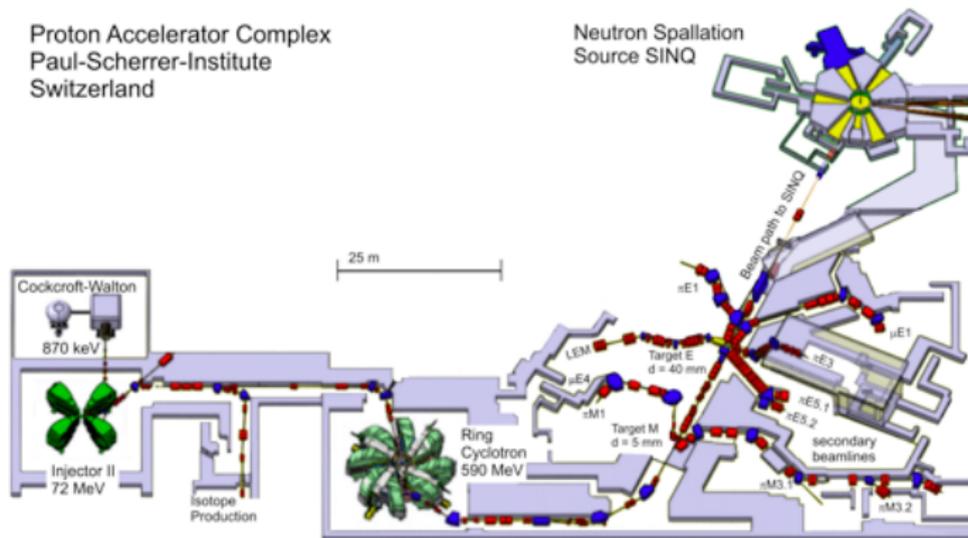
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PSI HIPA Overview

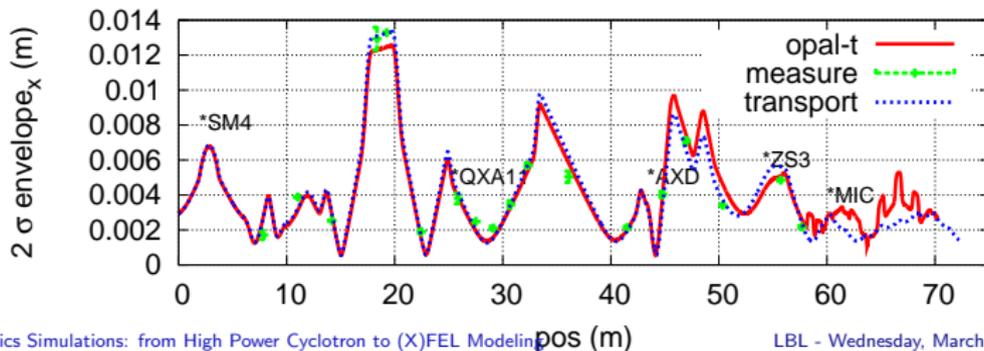
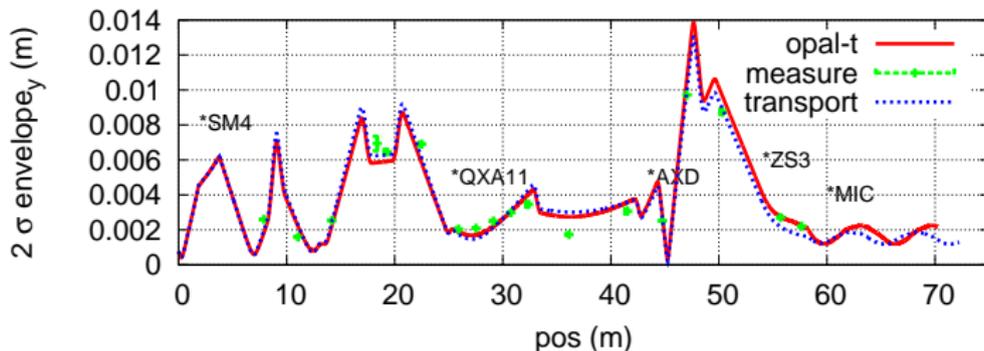
Proton Accelerator Complex
Paul-Scherrer-Institute
Switzerland

Neutron Spallation
Source SINQ

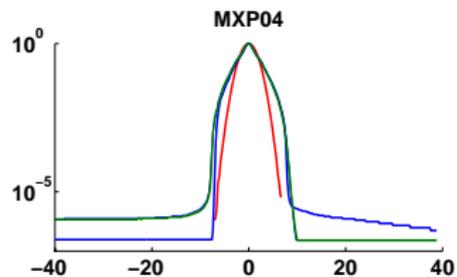
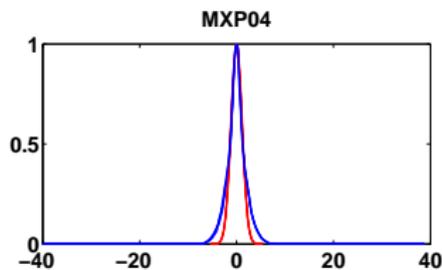
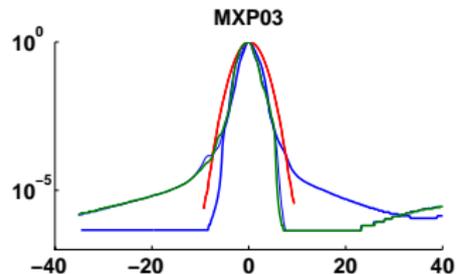
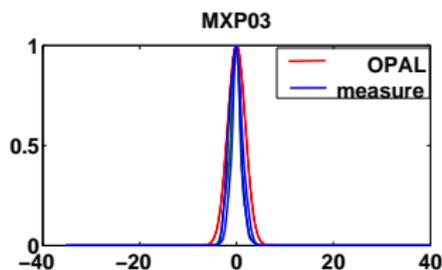


OPAL-T Simulations of the PSI IW2 Line (72 MeV p)

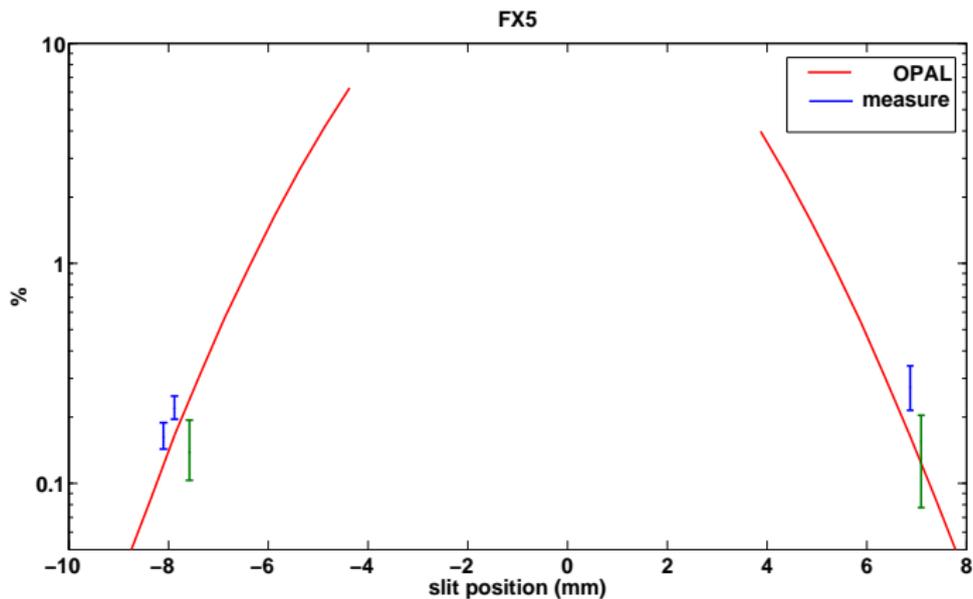
Production run setup (2.2 mA)



Comparison of beam profile monitors in the PSI-IW2 Line

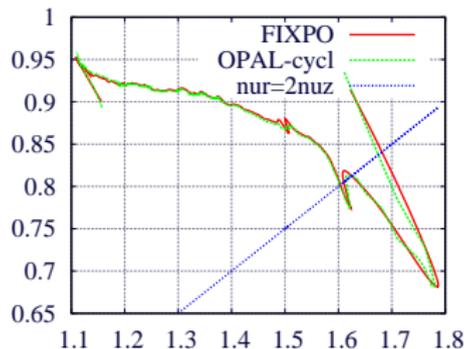
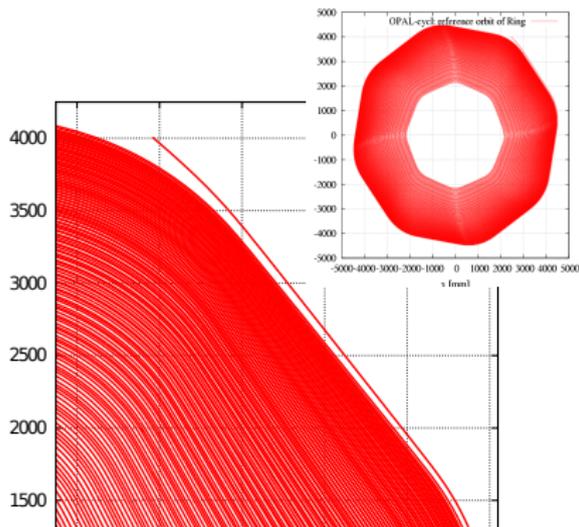


Comparison of beam losses on the slits with measurements

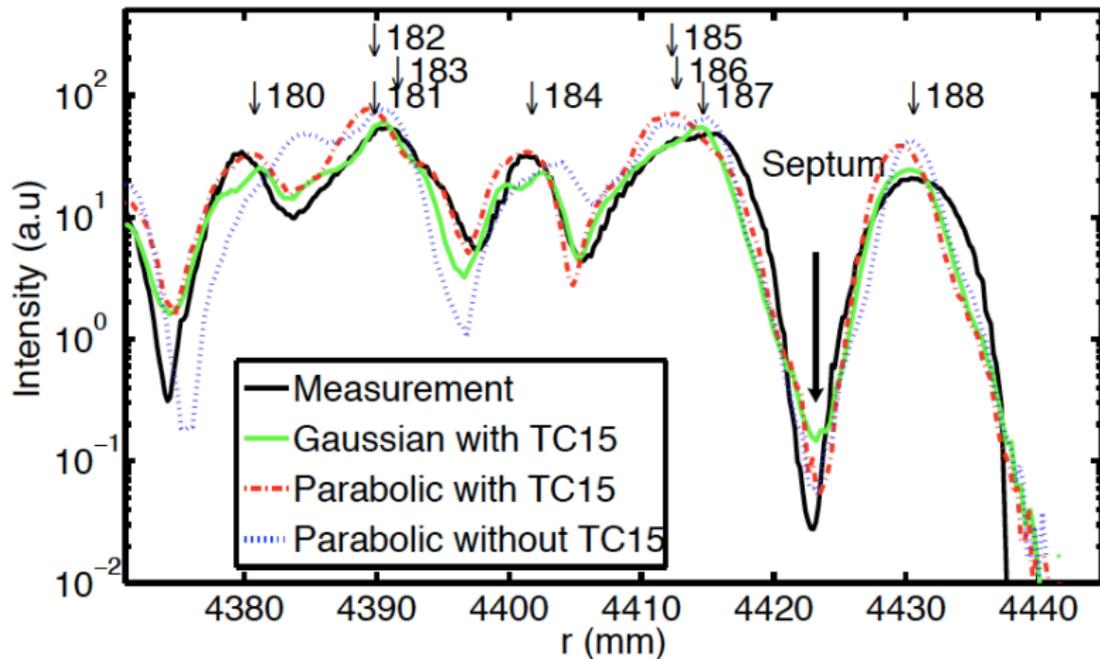


PSI 590 MeV Ring - last 8 turns

- initial conditions from 72 MeV transfer line simulation (OPAL-T)
- rf parameters from control room
- using measured mid-plane field and analytic trim-coil (tc15)
- single particle run to verify tun numbers and tunes



PSI 590 MeV Ring - last 8 turns @ 2.2 mA

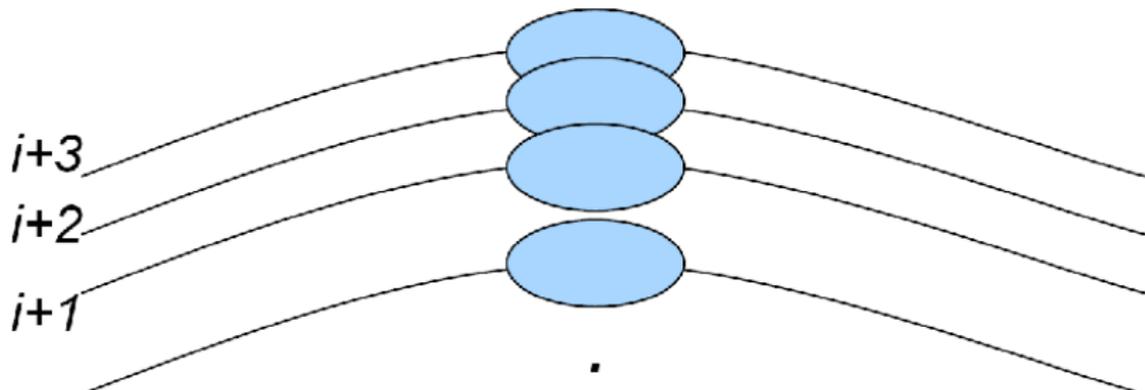


[Y. Bi, A. Adelman]

Neighboring Bunch Effects- Multi Bunch Model

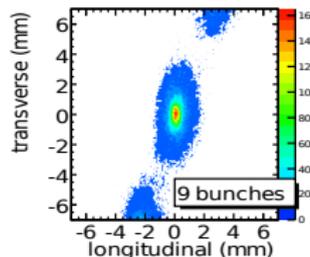
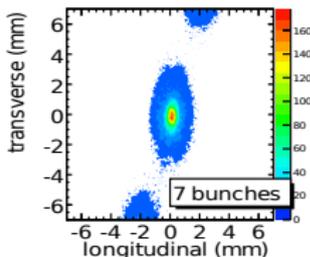
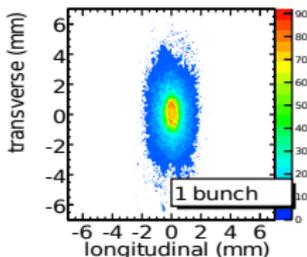
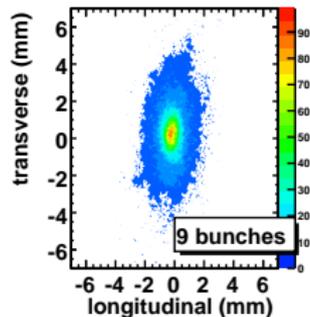
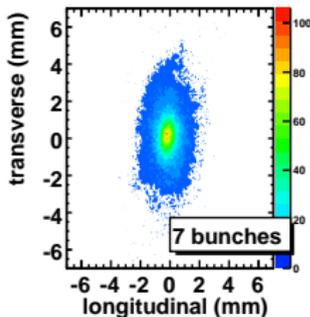
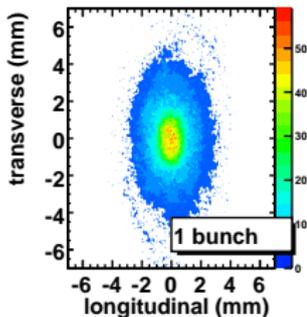
In the model, the injection-to-extraction simulation is divided into two stages:

- ① First stage, big $\Delta r \Rightarrow$ single bunch tracking
- ② Second stage, small $\Delta r \Rightarrow$ multiple bunches tracking
 - Full 3D
 - Energy bins & re-binning
 - Large grids needed



PSI 590MeV Ring

Single bunch and multiple bunches at turn 80 and 130



[J. Yang, Adelmann]

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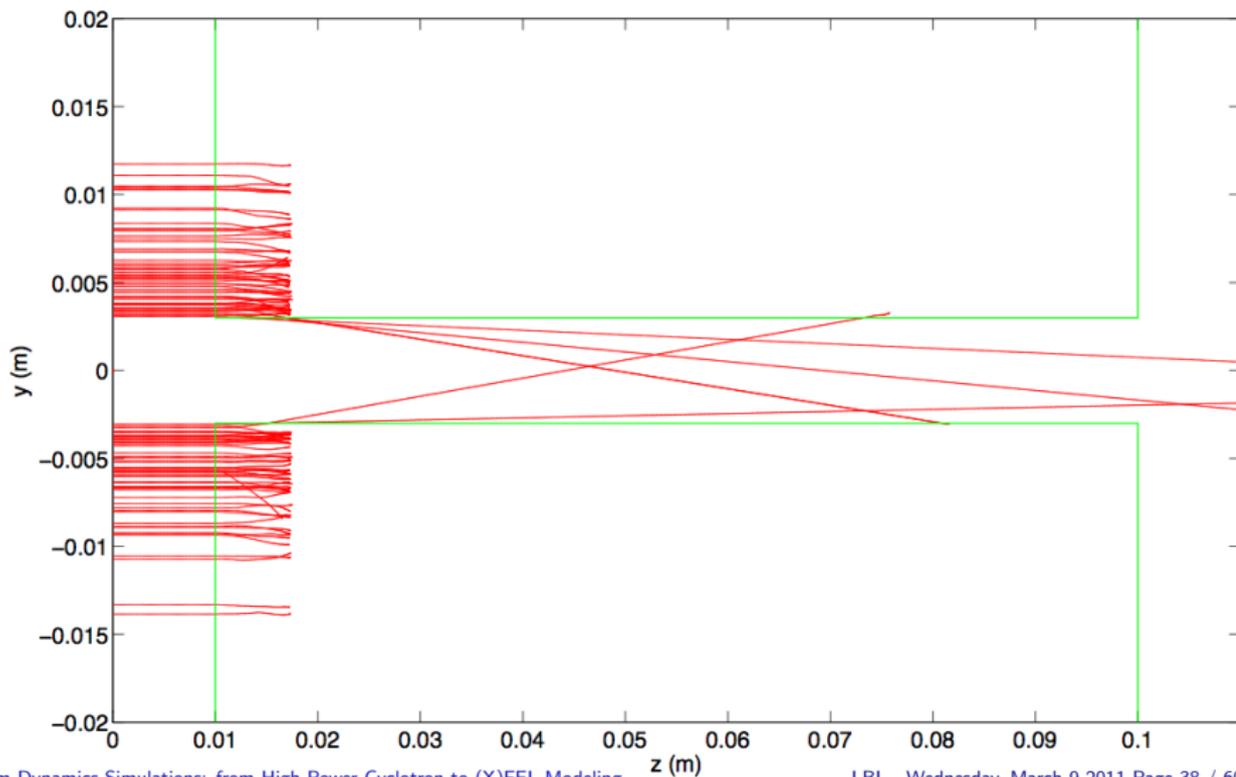
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Particle Matter Interaction

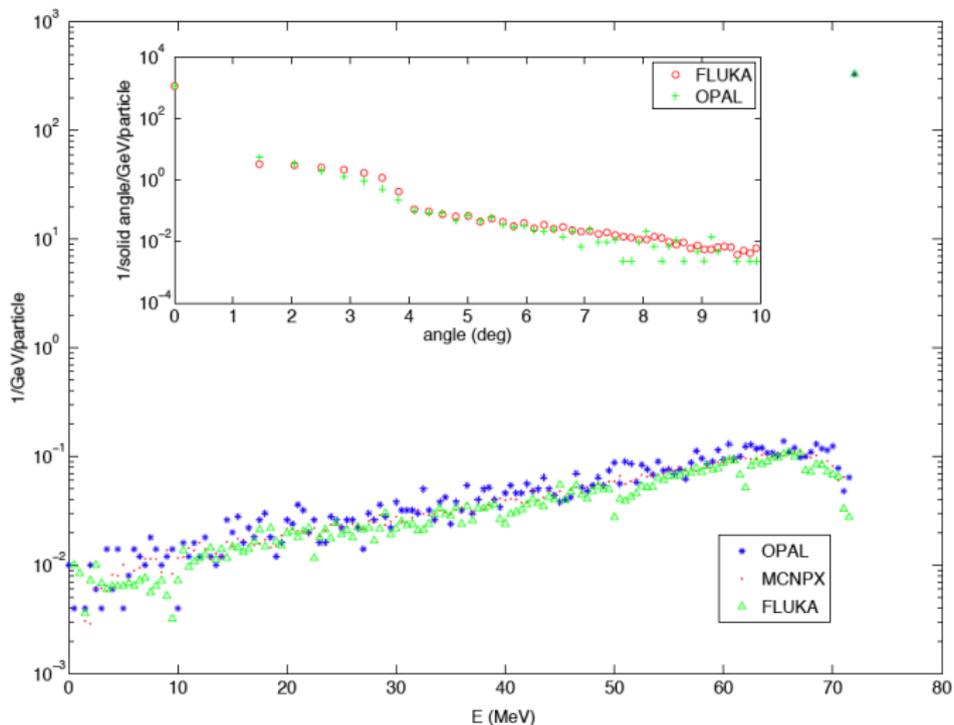
- Energy loss $-dE/dx$ (Bethe-Bloch)
- Coulomb scattering is treated as two independent events: the multiple Coulomb scattering and the large angle Rutherford scattering
- Space charge & halo generated by the obstacle

A 72 MeV cold Gaussian beam with $\sigma_x = \sigma_y = 5$ mm passing a copper slit with the half aperture of 3 mm from 0.01 m to 0.1 m.

Particle Matter Interaction cont.



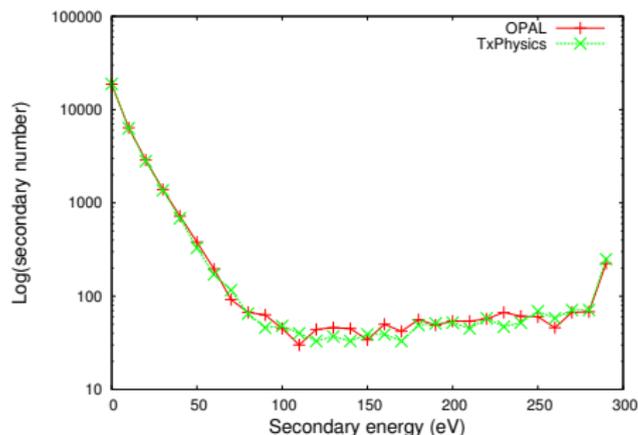
Particle Matter Interaction cont.



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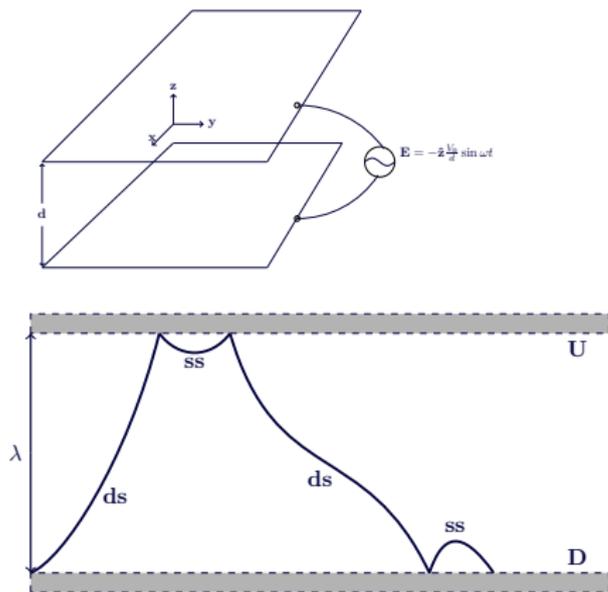
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Multipacting & Dark Current Modeling



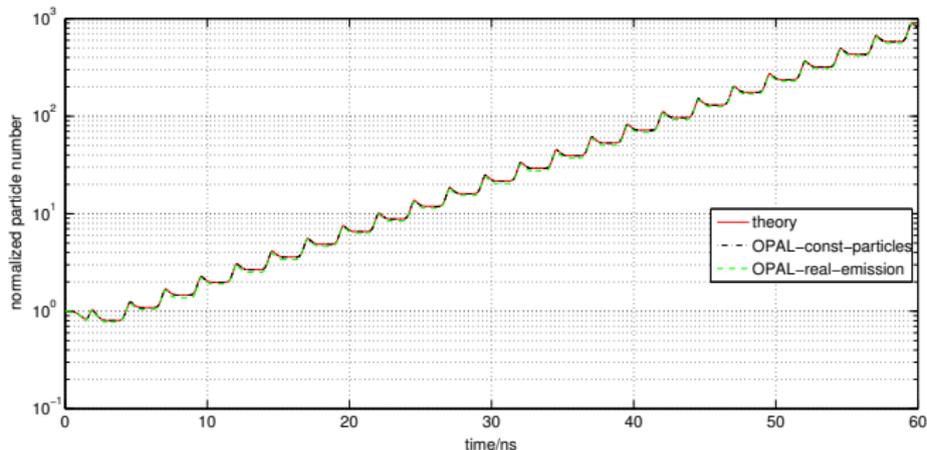
- Benchmark Against the TxPhysics Library
- Validate the implementation of Furman-Pivi's model
- Logarithm of total secondary emission number (backscattered + re-diffused + true secondaries) vs. energy of emitted particles

Multipacting & Dark Current Modeling cont.



- Benchmarking the secondary emission model is not sufficient!
- There double-side(ds) and single-side(ss) impacting exist
- This is the most complete description of multipacting [S. Anza et al]!

Multipacting & Dark Current Modeling cont.

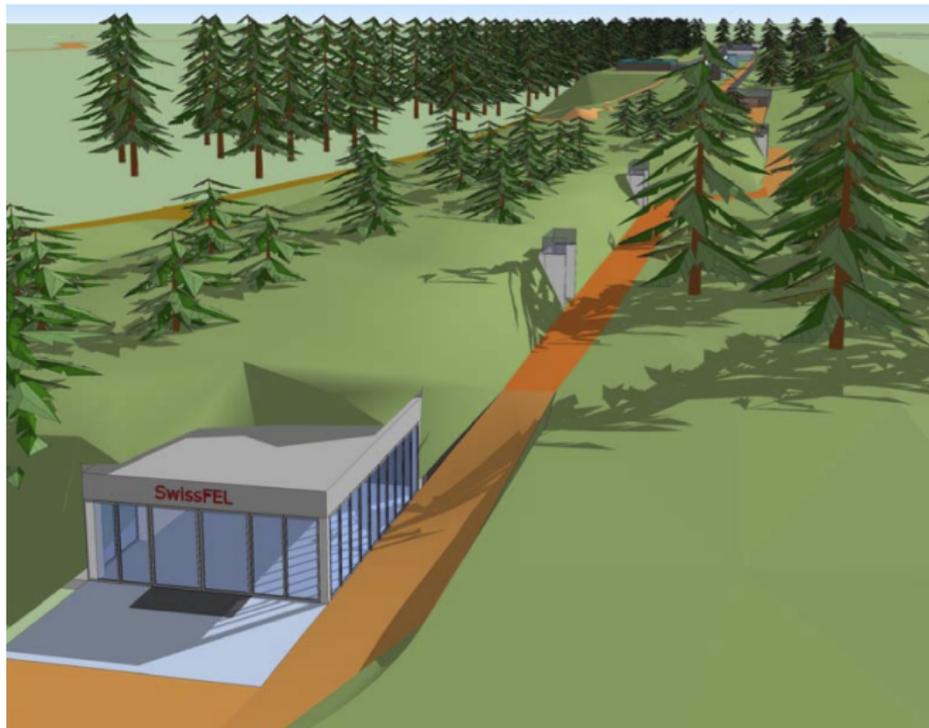


$f = 200\text{MHz}$, $V_0 = 120\text{V}$, $d = 5\text{mm}$, Furman-Pivi's model, copper and
 re-normalize to a const number of simulation particle

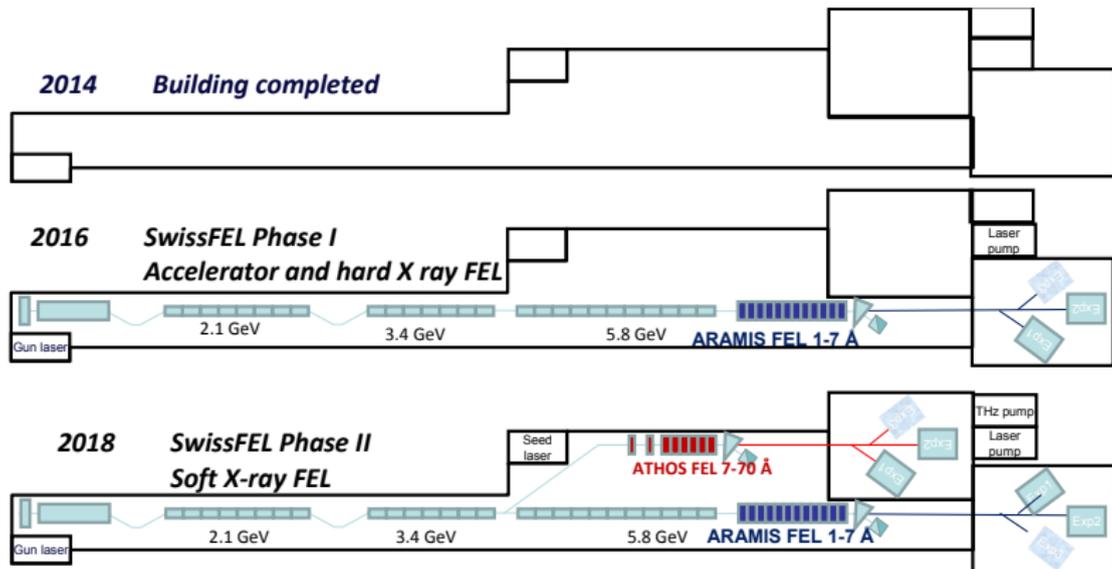
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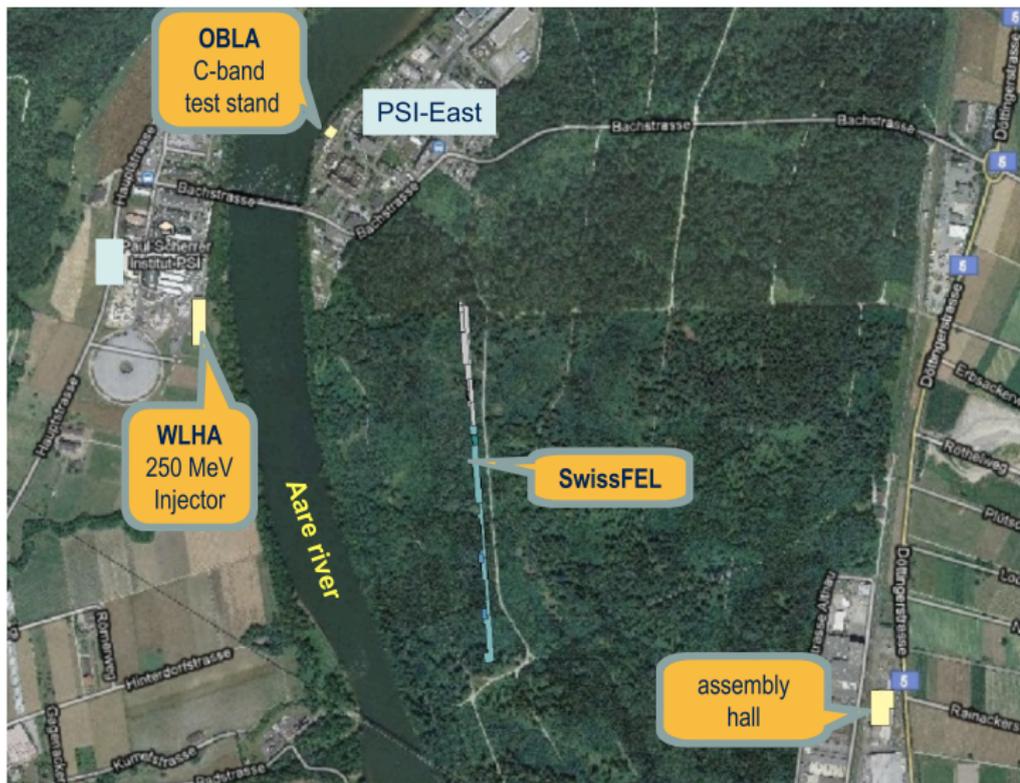
The SwissFEL <http://www.psi.ch/swissfel/>



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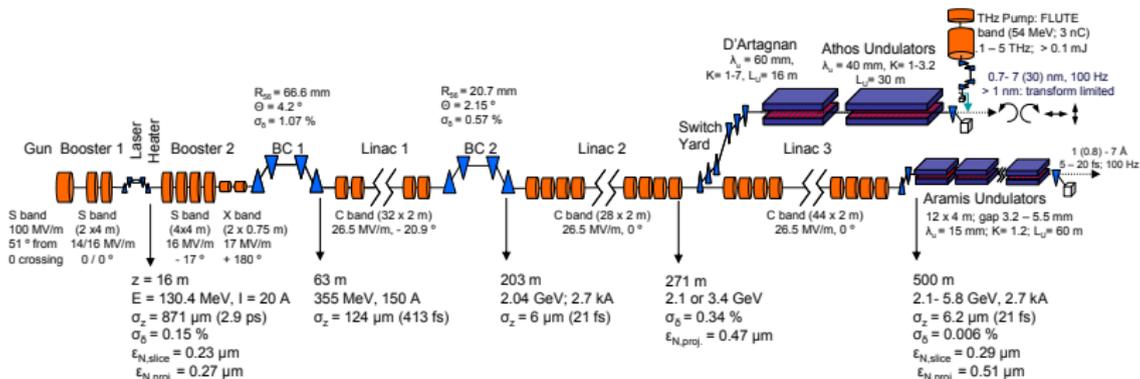
The SwissFEL cont.



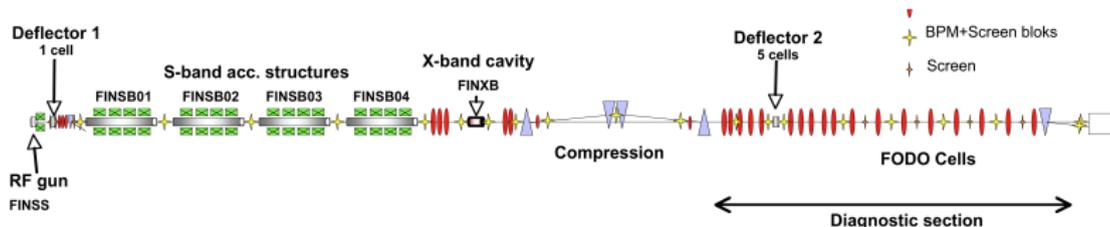
The SwissFEL cont.

E	5.8	(GeV)
P	5	(MW)
f_{rep}	100	(Hz)
λ	1...70	(Å)
L	713	(m)

- RF-Photo Gun (PSI development)
- frequency tripl. TiSa Laser
- S,C and X-Band RF structures
- norm. conducting



The 250 MeV Test Injector



What is primarily indispensable to get SwissFEL lasing?

Table: Critical Parameter to reach @ 250 MeV

Charge	20 pC	200 pC	
E	250	250	(MeV)
ΔE uncorr.	< 50	< 50	(keV)
ε_x rms proj	0.15	0.5	(mm-mr)
ε_x slice	0.11	< 0.4	(mm-mr)
I peak	100	350	(A)

Benchmarking OPAL-T & Astra

OPAL-T simulation of the CTF3 gun and 2 S-band TW structures and solenoids.

Table: Initial conditions

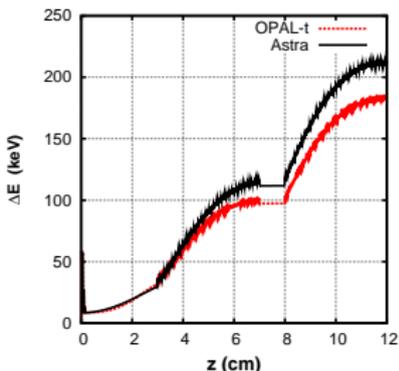
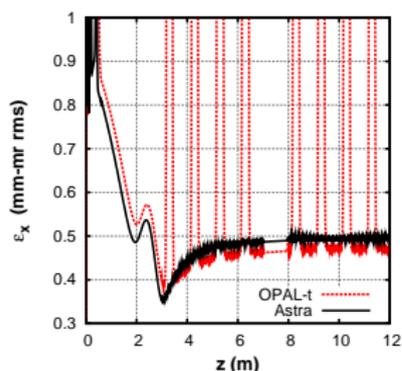
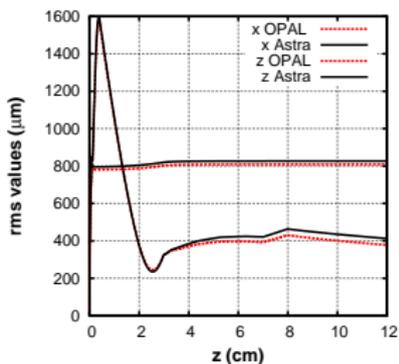
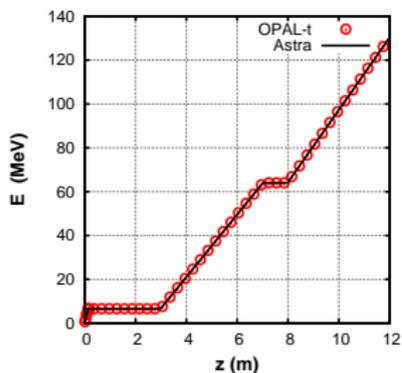
σ_x	249	μm
σ_y	249	μm
Q	200	pC
t_{fwhm}	9.9	ps
$t_{\text{rise}} = t_{\text{fall}}$	0.782	ps
E_{th}	0.65	eV
ϕ_{gun}	-3.5	deg
ϕ_{tw1}	0.0	deg
ϕ_{tw2}	0.0	deg

Table: $Q = 200$ pC at 12m

	OPAL	Astra	
E_{final}	130.249	130.290	(MeV)
ΔE_{final}	184.79	213.22	(keV)
ε_x rms	0.46990	0.49075	(mm-mr)
x rms	377.648	412.510	(μm)
z rms	809.092	826.860	(μm)

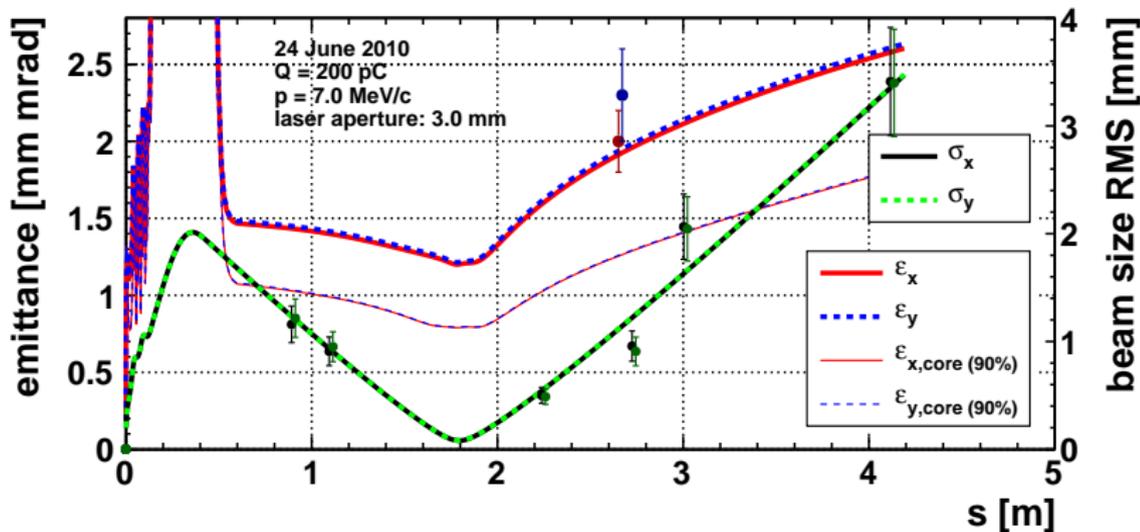
Both codes run autophase

Benchmarking OPAL-T & Astra cont.

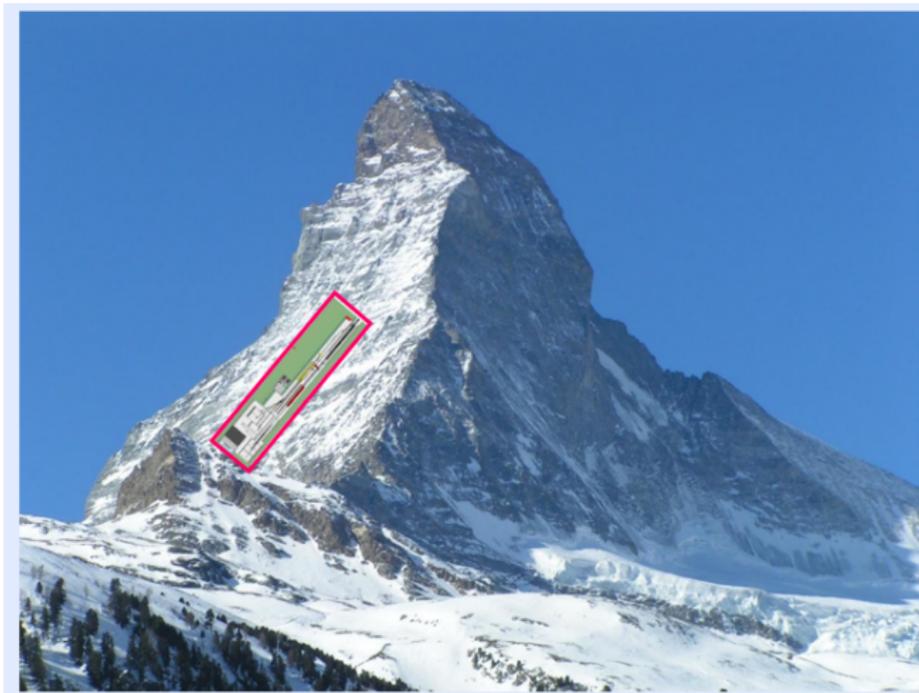


Comparing Simulations with Reality

OPAL-T simulation of the CTF3 gun, including thermal emittance (0.65 eV) and laser profile (0.7 ps rise time 9.8 ps flat-top).



The SwissFEL is a very compact machine



J. Rossbach / Univ. HH&DESY - Inauguration SwissFEL Injektor 24.8.2010

References

-  A. Adelman, P. Arbenz and Y. Ineichen, J. Comp. Phys, 229 (12): 4554-4566 (2010)
-  M. A. Furman and M. Pivi, Phys. Rev. ST Accel. Beams 5, 124404 (2002)
-  S. Anza, C. Vicente, J. Gil, V. E. Boria, B. Gimeno, and D. Raboso, Phys. Plasmas 17, 062110 2010
-  Y. Bi, A. Adelman et.al submitted Phys. Rev. STAB and <http://arxiv.org/abs/1012.0718>
-  J. Yang, Adelman et.al, Phys. Rev. STAB Volume 13 Issue 6 064201 (2010)
-  J. R. M. Vaughan, IEEE Transactions on Electron Devices 40, 830 (Apr 1993)

Backup

```
GME:GEOMETRY, LENGTH=1, S=0.0, A=0.00085, B=0.00085;

Fs1:FIELDSOLVER, FSTYPE=MG, MX=32, MY=32, MT=64,
      PARFFTX=false, PARFFTY=false, PARFFTT=true,
      BCFFTX=dirichlet, BCFFTY=dirichlet, BCFFTT=open,
      GEOMETRY="GME", ITSOLVER="CG", INTERPL="linear",
      TOL=1e-6, MAXITERS=100, PRECMODE="reuse";

Fs2:FIELDSOLVER, FSTYPE=FFT, MX=32, MY=32, MT=64,
      PARFFTX=false, PARFFTY=false, PARFFTT=true,
      BCFFTX=open, BCFFTY=open, BCFFTT=open,
      BOXINCR=1.0, GREENSF=INTEGRATED;

beam1: BEAM, PARTICLE=ELECTRON, PC=P0, NPART=1e5,
      BFREQ=1498.953425154e6, BCURRENT=0.299598, CHARGE=-1;

SELECT, LINE=FIND1;
```

```
TRACK,LINE=FIND1, BEAM=beam1, MAXSTEPS=10000, DT=1.0e-12;  
  RUN, METHOD = "PARALLEL-T", BEAM=beam1,  
  FIELDSOLVER=Fs2, DISTRIBUTIONS={Dist1,Dist2};  
endtrack;
```

```
f1: Filter, TYPE="FixedFFTLowPass", NFREQ=9;  
f2: Filter, TYPE="Savitzky-Golay", NLEFT=64,  
NRIGHT=64,POLYORDER=1;  
CSRWAKE: Wake, TYPE="1D-CSR", FILTERS={f2, f1};
```

```
F10BC_MB01: RBend, L=0.282000, K0=0.1585,  
FMAPFN="F10BC-MB01.T7", ELEMEDGE=29.964,  
ALPHA=3.035, DESIGNENERGY=247.6, WAKEF=CSRWAKE;
```

```
KX1I_PHYS: SurfacePhysics, TYPE="Collimator",MATERIAL="Cu";

KX0I: ECollimator, L=0.09, ELEMEDGE=0.01,
XSIZE=0.003, YSIZE=0.003,
APERTURE={0.003,0.003},SURFACEPHYSICS='KX1I_PHYS';

DR1:DRIFT, L=0.09, ELEMEDGE=0.01,
APERTURE={0.003,0.003}, SURFACEPHYSICS='KX1I_PHYS';

QXA1:QUADRUPOLE,L=0.19,ELEMEDGE=0.11,K1=1.0,
APERTURE={0.003,0.003}, SURFACEPHYSICS='KX1I_PHYS';

MXP00: Monitor, L=0.002, ELEMEDGE=0.1, OUTFN="MXP00.h5";

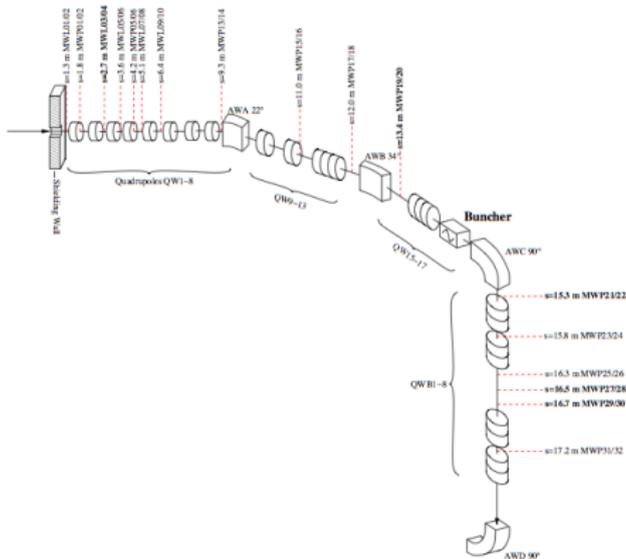
IW2Line: Line=(MXP00,KX0I);
```

870 keV Injection Line

Simulation and measurement DC beam 870 keV

Find D_{start} and ν_e by $\min(F)$:

$$F = \sum_{n=1}^{\#monitors} (\tilde{\chi}_{mea}(s_n) - \tilde{\chi}_{sim}(s_n))^2.$$

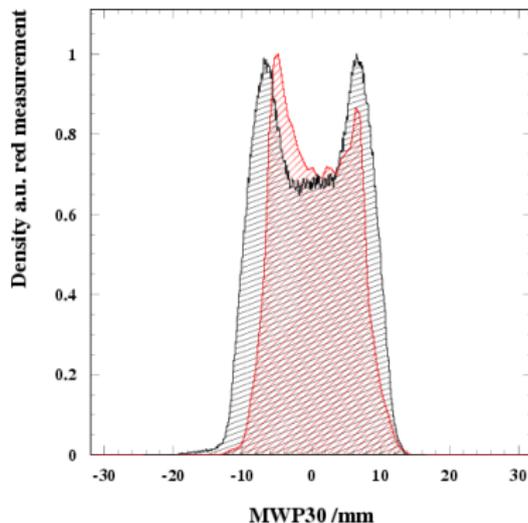


870 keV Injection Line

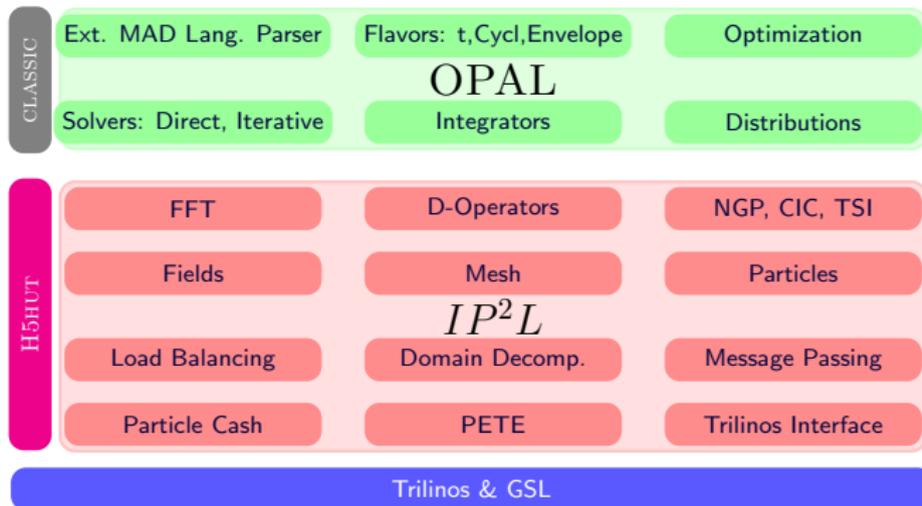
Simulation and measurement DC beam 870 keV

Find \mathcal{D}_{start} and ν_e by $\min(F)$:

$$F = \sum_{n=1}^{\#monitors} (\tilde{\mathcal{X}}_{mea}(s_n) - \tilde{\mathcal{X}}_{sim}(s_n))^2.$$



OPAL Architecture



- **OPAL Object Oriented Parallel Accelerator Library**
- **IP²L Independent Parallel Particle Layer**
- Class Library for Accelerator Simulation System and Control
- **H5hut for parallel particle and field I/O (HDF5)**
- **Trilinos** <http://trilinos.sandia.gov/>

OPAL Parallel Scaling on Cray XT5 (FFT Solver)

- Tracking 10^8 Gaussian distributed particles
- 3D FFT on a 1024^3 grid

